



An analytical approach to activating demand elasticity with a demand response mechanism



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ABSTRACT

The aim of this work is to demonstrate analytically the conditions under which activating the elasticity of consumer demand could benefit social welfare. We have developed an analytical equilibrium model to quantify the effect of deploying demand response on social welfare and energy trade. The novelty of this research is that it demonstrates the existence of an optimal area for the price signal in which demand response enhances social welfare. This optimal area is negatively correlated to the degree of competitiveness of generation technologies and the market size of the system. In particular, it should be noted that the value of unserved energy or energy reduction which the producers could lose from such a demand response scheme would limit its effectiveness. This constraint is even greater if energy trade between countries is limited. Finally, we have demonstrated scope for more aggressive demand response, when only considering the impact in terms of consumer surplus.

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1. Introduction

The deployment of smart grids is seen as heralding a major change in electricity markets. One of the main considerations, presented as a necessary condition to benefit from this development, is to be able pilot demand or make it respond to price or market constraints (Chao, 2011). Setting aside any improvements in network management, consumer behaviour will have a key impact on uses and investment-planning in the midstream (networks) and the upstream (generation) (Strbac, 2008). The idea is to replace some of the heavy investment in infrastructure by a reduction in consumption. This could be done by consumers or another body (aggregators, suppliers, or distributors) on behalf of consumers. Experiments have shown that investing in smart-grid technology could be cheaper than heavier investments in infrastructure (Kema, 2012).

The main feature of electricity demand is its inelasticity (Stoft, 2002). Currently, most electricity consumers are captive in the short term. Industrial customers could be more volatile, but mainly in the long term (Lijesen, 2007; Patrick and Wolak, 2001). However, the aim of deploying smart grids and demand response (DR) schemes is to

introduce short-term elasticity into some uses. In this way, issuing price signals to consumers will always reduce consumption.² The literature generally shows that demand is elastic when a dynamic tariff is introduced. However, the value of the elasticity varies depending on several factors, such as the period of consumption, household appliances, degree of deployment of smart-grid technologies, or the price differential between periods of consumption (Boisvert et al., 2004; Di Cosmo et al., 2014; Faruqui and Sergici, 2010). Several papers have studied the impact of dynamic pricing on consumers and markets design to remunerate curtailments. Chao (2011) has demonstrated that, in a perfect competitive market, remuneration of curtailment is equivalent to the difference between the retail rate and the real-time price should be optimal for welfare. Orans et al. (2010) show that a three-part tariff, including time-of-use, a fixed fee, and DR remuneration, is an efficient tool for providing consumers with an incentive to change their behaviour.

We draw on these papers using analytical equilibrium in interconnected markets to study the cases in which an increase in tariffs would reduce consumption without jeopardizing social welfare. We use a deterministic optimization model with supply functions (Ventosa et al., 2005). As in other papers (Stoft, 2002), we assume perfect competitive markets. Each producer bases its bids on its marginal costs, as in Woo (1990) and De Jonghe et al. (2011). However, to our

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² This result could be overcome by extending the rebound effect (Muratori et al., 2014).

knowledge, only a few works have sought to analytically model the deployment of demand response in the context of interconnected electricity markets. [Vespucci et al. \(2013\)](#) is the model closest to ours. A large part of their analysis focuses on the transformation of their optimization problem into a linear one, as electric supply and demand functions are discontinuous. They also demonstrate, with application data, that a dominant firm always has an incentive to use market power to achieve higher profit targets. Our model differs from theirs on two points. Firstly, we compute theoretical equilibria in the context of two interconnected markets with several technologies in each market. Secondly, we introduce an analysis of demand response (DR) linked to the degree of the elasticity of consumer demand. [Léautier \(2014\)](#) has also studied, using an analytical approach, the impacts on welfare of switching from inelastic to elastic demand via the application of real-time pricing scheme.³ Our analysis extends this work by addressing the effectiveness of demand response when several markets, using different generation technologies, are interconnected. It adds to this literature on considering the extent to which the effectiveness of a demand response should consider the system's interactions with foreign systems through the energy exchanges and the difference between the generation technologies mix.

In our research work, we focus on the effectiveness of deploying a demand response scheme. We may assume that widespread application of DR would have several impacts on system equilibrium. The main objective of this scheme is to make consumers sensitive to prices in the short run.⁴ They could actively participate in managing system security, instead of relying only on supply management when the system is close to rationing. DR schemes offer consumers an incentive to adopt a degree of flexibility in their consumption. Each part of the electricity supply chain would benefit from this flexibility, gaining in efficiency.

Deploying a mechanism of this sort would nevertheless have a high cost. Consumers need to adapt and modify their behaviour, switching from being captive and non-elastic to being genuinely elastic. It is worth noting that under a DR scheme, demand becomes elastic for a large range of consumers, independently of their own appliances. As several pilot schemes in the US have shown ([Faruqui et al., 2009](#)), the main gains are obviously achieved at peak hours. Demand for electrical heating or air conditioning are the main categories of consumption which could be managed under DR schemes. However, dynamic pricing gives a large share of consumers an incentive to reduce consumption, regardless of whether they own air conditioning, for example ([Di Cosmo et al., 2014](#)). Information technology, such as home displays, increases such effects, providing continuous information to customers on consumption and tariffs. The impact of DR schemes on price bids has been studied in the literature. DR is a key factor in making smart grids work because it allows efficient interaction between the segments of the electricity supply chain.⁵ The literature has studied a variety of DR tools ([Bergaentzle et al., 2014](#); [Faruqui and Sergici, 2010](#); [Horowitz and Lave, 2014](#)), going from the simplest mechanism which involves dividing periods of consumption into price blocks, in which the price increases in step with short-term system vulnerability (time-of-use or critical peak pricing), to more complex systems in which consumers respond to electricity prices in real time (real-time pricing). When several communications technologies are developed, load management of

consumers by the supplier or the distribution system operator would allow a significant decrease in demand, higher than a reduction managed only by the consumer. All these tools imply an increase in electricity prices at times of high demand and lower prices at other times. It seems realistic to assume that activating DR will result in an increase in electricity prices in peak periods. As prices increase, some consumers could be worse off due to this increase ([Horowitz and Lave, 2014](#)). As the main gain from a DR scheme is a drop in peak-load demand, incentive prices or direct load control are used to make the volume effect greater than the price effect; in other words, decreasing electricity consumption compensates for increasing prices. This should be done by minimizing the impact on consumer utility,⁶ as consumers must have incentives to participate in a DR scheme. We shall therefore study two economic indicators—social welfare and consumer surplus—to gauge the efficiency of the DR schemes.

In our paper, we model a system in which generators, integrated with suppliers or retailers, make bids (supply curves) to the system operator which maximizes the welfare balancing offer and demand. With SG technologies, consumers could become active on the market; thus, their demand function becomes elastic. In this environment, we start by analysing the way the structure of generating technologies could affect merit orders in different countries and potential trade between them. Our results show that the trade-off between producing locally and exporting energy depends on the opportunity cost of the energy and the overall efficiency of generating technologies. Then, we demonstrate that there is an optimal level for the price signal at which DR increases social welfare. We use computed equilibria from our initial analysis to show that this optimal level is negatively correlated to the degree of competitiveness of the generating technologies and the size of the market. The value which producers could lose due to unserved energy or energy reductions would limit the deployment of a scheme of this sort. Moreover, this constraint is greater if energy trade between countries is limited. However, the constraint is less acute if the considered system is cost-inefficient, with only limited connections with neighbouring systems.

The paper is divided into five sections. Following this introduction, [Section 2](#) presents the assumptions used in modelling the analytical equilibria and results of social-welfare analysis. [Section 3](#) focuses on the effectiveness of DR with regard to consumer-surplus criteria. [Section 4](#) analyses the sensitivity of the results to the elasticity of demand. [Section 5](#) presents our conclusions.

2. A model for demand response

2.1. General assumptions

2.1.1. Trade between the systems

We shall assume there are two interconnected countries⁷ ($n = 1, 2$).⁸ Each system operator balances total supply and demand, making allowance for possible trade between the countries. Such trade is limited by an interconnection capacity between country n and m , $Cap_{n,m}$, which has a price $P_{n,m}$ when capacity is saturated.

2.1.2. Generation technologies and supply

Each country is characterized by the presence of t generation technologies, $t = \{1 \dots k\}$. We assume perfect competition in both markets.⁹

³ [Léautier \(2014\)](#) applies his results to the French market. As marginal revenue of SG deployment is decreasing, current costs of marginal deployment of smart meters are too high compared to benefits. Thus, it should be not profitable to continue to install equipment for all consumers. Moreover, [Crampes and Léautier \(2015\)](#) have recently shown that under imperfect information, DR could reduce the welfare from the adjustment market as consumers could behave strategically.

⁴ Electricity consumers are recognized to be elastic only in the long run, even if in the short run, some of them can be partly elastic too. We also note that we make no distinction between residential and industrial consumers, who have different consumption profiles and would, in practice, react differently to an intensive DR scheme.

⁵ For instance, generators of conventional or intermittent energies could easily manage variations in their production and integrate renewable energies in the power system.

⁶ One of the main fields of research by suppliers is for ways of convincing consumers to participate in DR schemes. To gain consumer acceptance, DR schemes must minimize impact on both modern amenities and electricity bills.

⁷ The model could be enlarged to analyse more than two interconnected systems.

⁸ Index m is also used.

⁹ We disregard the strategic behaviour of producers by assuming that the merit order of a given system is the result of aggregating the marginal costs of available generation technologies. The model is a one-shot game with linear demand. To serve demand, all capacities are offered to the market through the aggregate supply function.

Each technology is characterized by a quadratic variable cost function,¹⁰ described as follows:

$$CV_{t,n}(x_{t,n}) = a_{t,n}x_{t,n} + \frac{1}{2}b_{t,n}x_{t,n}^2 \quad (1)$$

$a_{t,n}$ and $b_{t,n}$ are parameters and $x_{t,n}$ is the quantity produced by technology t in a given country n .

By aggregating the marginal costs of the technologies available in country n , we obtain the following inverse supply function:

$$S_n(X_n) = a_n + b_n X_n \quad (2)$$

a_n and b_n are aggregate parameters and $X_n = \sum_{t=1}^k (x_{t,n} + x_{t,n,m})$ is the total quantity produced in a given country n , with $x_{t,n,m}$ the quantity produced by technology t in a given country n and exported towards country m . See Appendix 1 for more details on construction of the supply function.

For simplicity's sake, we shall rank the technologies from the least to the most expensive.¹¹ A linear relationship between the variable costs function of the technologies is made as follows:

$$a_{t,n} = \alpha^{t-1} \cdot a \quad \text{and} \quad b_{t,n} = \alpha^{t-1} \cdot b$$

where α is a ranking parameter of the technologies¹²; a and b correspond to the parameters of the least expensive technology.

2.1.3. Demand and market equilibrium

In the first scenario, electricity demand in a given country is assumed to be inelastic (\bar{D}_n). In the second scenario, we assume that implementing a demand response mechanism will modify consumer behaviour, so that demand becomes elastic. The inverse demand function in the latter case is given by

$$D_n^{-1}(X_n) = c_n - d_n X_n \quad (3)$$

where c_n and d_n are the parameters of the inverse demand function.

Market equilibrium is found at the intersection between the supply and demand functions (Fig. 1). As long as consumers remain passive players, their demand function just depends on prices and their elasticity. The supply function is the result of a minimization program by which the system operator determines the aggregate supply function to be minimized to satisfy local demand. As in Vespucci et al. (2013), this minimization includes local generation technologies and potential import from the neighbour country (see Section 3).

Final consumption in a given country Q_n will take this form:

$$Q_n = \begin{cases} \bar{D}_n & \text{if Demand is inelastic} \\ D_n^{-1}(Q_n) & \text{if Demand is elastic} \end{cases} \quad (4)$$

2.1.4. Modelling demand response

Let us assume that widespread application of DR will lead to at least two consequences in the future. Firstly, we may posit that the additional cost of DR borne by suppliers will modify and increase their supply function. Investments in metering, energy boxes, and sensors will be needed to precisely assess energy consumption and maximize the impact of DR schemes. Firms should also invest in people to manage big data and pilot the DR scheme. All these investments will need to be recouped by the firms, leading to higher fixed and variable costs. Suppliers will undertake such investments after estimating their specific market

share whereas the cost will be transferred to consumers by a tariff increase. The case studied in our model, as in Crampes and Léautier (2015), could be seen as a supplier vertically integrated in generation. This supplier sends a price signal to the consumer, a signal composed by smart appliances costs and others features of the market. As perfect competition is assumed, the supply function of the integrated entity should integrate supply costs plus the costs of smart appliances that should be recovered through its supply activity.¹³ Finally, these costs are paid by consumers. Thus, this could be modelled by assuming that the technology's operational costs (Eq. (1)) will increase by a convex function, $\frac{1}{2}\gamma_n x_{t,n}^2$ where γ_n can be interpreted as a DR intensity parameter.¹⁴ This parameter contains all costs of the DR program as well as the intensity of the price signal given to consumers. We therefore assume a positive correlation between the intensity of suppliers' investments in the smart-grid system and the opportunity for consumers to manage their consumption with a wide range of tools (in-home display, direct load control, energy boxes, etc.). On the other hand, we can assume that consumers, now being price-sensitive, will become demand-elastic. Graphically, the electricity price shifts from point A to point B, as shown in Fig. 1 above, as it moves from a no-DR scenario to a widespread-DR scenario. With deployment of smart grids, consumers receive information, allowing them to make decisions, change their patterns of electricity consumption and adapt their demand. DR schemes change the cost of electricity for consumers: they receive new price signals, given by their suppliers, and, with new SG technologies, they can respond to them. The reserve price for consumers with DR, c_n , is now higher than $Voll_n$. Indeed, when consumer demand is price-elastic, consumers are inclined to pay higher prices for electricity when the system is rationed, so they attach a much higher value to electricity scarcity which implies an increase in the value of lost energy ($Voll$).¹⁵

We shall consequently study the impact of price-based DR on the market equilibrium of two interconnected areas, with regard to social welfare and consumer surplus. We first consider the most the system operator can reduce demand without any loss in social welfare. We define $Q_{n,min}$ as the minimum consumption we can reach without decreasing social welfare. Then, we introduce analysis of consumer surplus to show that some types of DR scheme may not degrade this surplus. We also carry out sensitivity analysis of key parameters and the level of demand elasticity.

2.2. Welfare-related analysis of the impact of demand response

2.2.1. Baseline case

We start from the scenario without demand response. Since demand is inelastic, optimal production and trade maximizing social welfare (5) are the solution of the following program:

$$\text{Max}_{x_{t,n}, x_{t,n,m}} \int_0^{\bar{D}_n} (Voll_n - S_n(X_n)) dX_n \quad (5)$$

¹³ Several operators or actors could invest in smart technologies or smart appliances: suppliers/retailers, consumers, aggregators of flexibility, etc. Our model only considers the investment made by suppliers. We do not capture those made by aggregators or directly by consumers. Smart Grid investments can be seen as any other classical investment in innovation. It's firstly assumed by suppliers or grid companies and then passed through to consumers via an increase in the regulated tariffs or directly in electricity prices. Moreover, pilots on smart grids have shown that utilities make the investment that is more often a private one (with a complement of public funds). An exception is on smart meters that are supported by DSO (Gangale et al., 2013; Greening, 2010). We are grateful to an anonymous referee for this remark improving the understanding of the research.

¹⁴ The more the investment in smart appliances is, the more the demand response could be high. The degree of smart investment is positively correlated to the potential of DR. Thus, γ_n captures this relationship and its meaning could be analysed as the intensity of the DR program.

¹⁵ In practice, the reserve price varies with the type of consumers, their elasticities as well as the duration of the outage (Léautier, 2012).

¹⁰ Assuming a perfect competitive market, fixed generation costs are disregarded, having no impact on our results.

¹¹ The efficiency of generation technologies relies on input costs, yields, other variable costs to produce one MWh, costs of emission trading system, the period of use, etc.

¹² We assume that α is slightly > 1 to keep a rational homogeneity in the generation technologies and avoid exponential disparity between them.

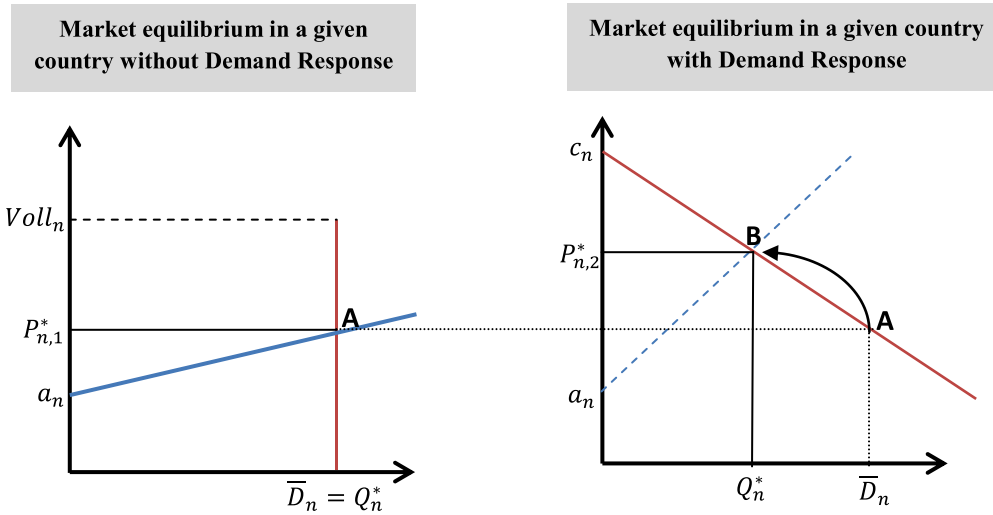


Fig. 1. Impact of a DR program on market equilibrium.

Subject to,

$$x_{t,n} + x_{t,n,m} \leq K_{t,n} \quad (r_{t,n}) \quad (6)$$

$$\sum_t x_{t,n,m} \leq Cap_{n,m} \quad (P_{n,m}) \quad (7)$$

$$\sum_t x_{t,n} + \sum_t x_{t,m,n} = Q_n \quad (f_n) \quad (8)$$

where,

- Cap_{n,m} Interconnection capacity between country *n* and country *m*
- X_{t,n} = x_{t,n} + x_{t,n,m} Total generation of technology *t* in country *n*
- K_{t,n} Available installed capacity of technology *t* in country *n*
- Q_n Final consumption in country *n*

Energy generation in a given country must comply with two constraints. First, the quantity generated by each technology *t*, which includes local generation, *x_{t,n}*, and possible exports to the neighbour country, *x_{t,n,m}*, cannot exceed available installed capacity (Eq. (6)). Secondly, energy exports from country *n* to country *m* are limited by the capacity of the interconnection line, *Cap_{n,m}* in Eq. (7). Finally, Eq. (8) shows that each system must balance its market by aligning local consumption, *Q_n*, with total energy fed into the system.

To solve the above constrained program, the equilibrium determines the optimal generation quantities, *x_{t,n}** and *x_{t,n,m}**, which simultaneously minimize the variable costs of generation in both countries. As demonstrated in Appendix 2, the solution is unique since the cost functions are strictly convex and continuously differentiable. The solution is found by regrouping all first-order conditions to form a mixed complementarity problem.¹⁶

Resolving the model as demonstrated in Appendix 3 implies the following main results:

Proposition 1. *The trade-off between producing locally or exporting energy would depend on the opportunity cost of energy and the overall*

efficiency of the production technology. Interconnection prices in both directions would limit trade between the countries. This impact is however weighted by the generation-costs differential between interconnected markets.

Optimal levels of production are defined as follows:

$$x^*_{t,n} - x^*_{t,n,m} = \frac{Q_n - Q_m}{\alpha^{t-1}} + \frac{(1-\alpha) \cdot \sum_n P_{n,m}}{\alpha^{t-1} \cdot (1-\alpha^t) \cdot b} \cdot \sum_t \frac{1}{\alpha_m^{t-1}} \quad (9)$$

Proof. See Appendix 3

When local consumption is higher than consumption in the foreign country: *Q_n ≥ Q_m*, the production which meets local demand *x_{t,n}** is far higher than the quantity exported *x_{t,n,m}**. In this case, the opportunity cost of selling energy to the local market is higher than exporting. Moreover, we can observe that the efficiency of technology *t* compared to the other technologies would influence the trade-off between producing locally and exporting. We assume that $\omega_t = \frac{\alpha^{t-1}}{\alpha-1}$ is the overall efficiency factor of technology *t*. This term ω_t also provides information on price levels in the two markets which balance supply and demand. So, according to this term, producers in country *n* must export capacity when their technologies are more efficient than those of their competitors in country *m*. The greater the efficiency of technology *t*, i.e. ω_t decreases, the more it will be preferred for balancing the system of the country with higher energy consumption.

The high values of *P_{n,m}* reduce the incentives for country *n* to export. The influence of the interconnection-capacity price on generation decisions is weighted by the efficiency factor of the technologies in the importing country defined by $\sum_t \frac{1}{\alpha_m^{t-1}}$. Thus, to maximize social welfare, it would be beneficial for country *m* with inefficient technologies to rely more on imports even with substantial interconnection prices, leading to an increase in *x_{t,n,m}**.

Proposition 2. *Efficient technologies would be called first to balance the markets. Other technologies would satisfy residual demand depending on their overall and relative efficiency. Trade would however be strongly correlated to interconnection prices and cost intensity in the importing country.*

¹⁶ Complementarity problems can be seen as expansions of square systems of nonlinear equations that include a mixture of equations and inequalities. It directly solves the necessary conditions of the mathematical programs. Writing and solving the first-order optimality conditions simultaneously for all programs results in a mixed complementarity problem.

Each efficient technology t would offer all its installed capacity to the interconnected markets. Optimal quantities for local production and for export are given as follows¹⁷:

$$x^*_{t,n} = \frac{K_{t,n}}{2} + \frac{Q_n - Q_m}{2 \cdot \omega_t} + \frac{\sum_n P_{n,m} \cdot \sum_t \frac{1}{\alpha_{t,m}}}{b \cdot \omega_t} \quad (10)$$

$$x^*_{t,n,m} = \frac{K_{t,n}}{2} - \frac{Q_n - Q_m}{2 \cdot \omega_t} - \frac{\sum_n P_{n,m} \cdot \sum_t \frac{1}{\alpha_{t,m}}}{b \cdot \omega_t} \quad (11)$$

We define \bar{t} as the index of inefficient technologies. They would only serve residual demand in the interconnected markets, with quantities lower than their total installed capacity. Their optimal production levels are given by¹⁸

$$x^*_{\bar{t},n} = \frac{Res_n - \phi_{\bar{t}}}{\omega_{\bar{t}}} + \frac{P_{n,m}}{b \cdot \omega_{\bar{t}}} \cdot \sum_t \frac{1}{\alpha_{t,m}} \quad (12)$$

$$x^*_{\bar{t},n,m} = \frac{Res_m - \phi_{\bar{t}}}{\omega_{\bar{t}}} - \frac{P_{n,m}}{b \cdot \omega_{\bar{t}}} \cdot \sum_t \frac{1}{\alpha_{t,m}} \quad (13)$$

where,

$$Res_n = Q_n - \sum_t x^*_{t,n} - \sum_t x^*_{t,m,n}$$

$$Res_m = Q_m - \sum_t x^*_{t,m} - \sum_t x^*_{t,n,m}$$

$\omega_{\bar{t}} = \frac{\alpha_{\bar{t}-1}}{\alpha_{\bar{t}}}$ where \bar{t} is the index of an inefficient technology

$\phi_{\bar{t}} = \sum_{\bar{t},n} \frac{a_{\bar{t},n} - a_{\bar{t},n}}{b}$ where \bar{t} is the index of the other inefficient technologies apart from \bar{t}

Proof. See Appendix 4

The call for a given technology to produce would depend on its efficiency compared to other technologies. When its efficiency is higher than a certain threshold, as discussed in Appendix 4, all its available capacity will be used to balance the systems. The other technologies will either fulfil the efficiency conditions and will hence be called at full capacity, or only serve residual demand, thus verifying the solution of Eqs. (12) and (13).

We shall now consider the efficient technologies. We can see that the share of capacity between local production and export is mainly determined by the energy-consumption differential, $Q_n - Q_m$. Generation is symmetrically shared between local generation and export, with a constant slope which depends on the overall efficiency factor of the technology, $\frac{1}{\omega_t}$; the total cannot exceed the available generation capacity, $K_{t,n}$. If technology t of country n is efficient with respect to other technologies, its production increases to serve both local demand and exports to neighbouring country m until its full capacity $K_{t,n}$ is reached. Generation sharing is impacted by the overall efficiency factor of the technology, ω_t . An increase in α^{t-1} , which means that the technology

tends to be more costly, leads to an increase in ω_t , meaning that the technology becomes less efficient. In this case, the incurred inefficiency will be borne by the system facing low demand. This behaviour should stop as soon as the overall inefficiency factor of efficient technology reaches a limit beyond which the technology becomes absolutely inefficient and will hence be shared, given the solutions to Eqs. (12) and (13).

As for inefficient technologies, their call is increasingly dependent on residual demand, as shown in Eqs. (12) and (13), and on the overall, $\omega_{\bar{t}}$, and relative, $\phi_{\bar{t}}$, efficiencies of the technology compared to the other inefficient ones. Not surprisingly, when choosing between inefficient technologies, the least inefficient ones are preferred, so $x^*_{\bar{t},n}$ and $x^*_{\bar{t},n,m}$ decrease when $\omega_{\bar{t}}$ or $\phi_{\bar{t}}$ increase. However, potential export is only impacted directly by the export capacity price, $P_{n,m}$. System operators will only rely slightly on inefficient generation technologies to balance their systems, so these technologies will only serve as auxiliary capacity.

In the sections and subsections that follow, the analysis of welfare, consumer surplus and elasticity will use the results of the equilibrium computed in Eqs. (10)–(13) and also refer to Fig. 1. Indeed, this figure illustrates how the elasticity of demand, consumer surplus and welfare levels could be modified given different parameters of costs, the level of market size and two configurations regarding the transmission capacity limits.

2.2.2. Introducing demand response

To assess the social efficiency of a DR scheme, we consider the maximum level of demand reduction the system operator can achieve without loss of social welfare. As we said previously, we define $Q_{n,min}$ as the minimum consumption above which social welfare does not decrease. As our model is on a single period, we could not capture the effect of load-shifting across several periods when DR occurs.¹⁹

We assume that the efficiency of a DR scheme would also depend on the competitiveness of the country concerned. We consequently consider two extremes cases separately: a cost-efficient country scenario; and a cost-inefficient country scenario.

The results of the previous sub-section highlight the impact of the opportunity cost of energy and the cost efficiency of technologies on energy trade between countries, subject to interconnection-capacity prices. The trade-off between costs and volume efficiencies would drive decisions on trade and generation. In the following we apply these theoretical predictions by considering the particular case of elastic demand with DR. The results of Propositions 1 and 2 will serve as the analytical basis for the following efficiency study.

We define Δ_n as the variation in welfare after deploying a DR scheme in country n as follows:

$$\Delta_n = SW_{n,2} - SW_{n,1} \quad (14)$$

where,

$SW_{n,1} = \int_0^{\bar{D}_n} (Vol_n - S_n(X_n)) dX_n$ social welfare at equilibrium before deploying the DR scheme.

$SW_{n,2} = \int_0^{Q_n} (D_n^{-1}(X_n) - S_n(X_n)) dX_n$ social welfare at equilibrium after deploying the DR scheme.

¹⁷ Providing $x^*_{t,n}$ and $x^*_{t,n,m}$ are non-negative, with $x^*_{t,n} + x^*_{t,n,m} < K$. Otherwise, if $x^*_{t,n} + x^*_{t,n,m} \geq K_{t,n}$, the equilibrium is $x^*_{t,n} + x^*_{t,n,m} = K_{t,n}$ and other technologies serve residual demand.

¹⁸ Providing $x^*_{\bar{t},n}$ and $x^*_{\bar{t},n,m}$ are non-negative and their sum does not exceed the technology capacity $K_{\bar{t},n}$. Otherwise, inefficient technologies produce at full capacity and there is a risk of an unbalanced market with no equilibrium.

¹⁹ However, load-shifting leads to greater demand in other periods. In our model, this implies two cases. If load-shifting impacts \bar{D}_n , an increase in demand raises $Q_{n,min}$ because of an increase in $SW_{n,1}$; thus shifting demand from one period to another one could be detrimental for welfare. If we consider that load-shedding only impacts elastic demand, the demand function $D_n^{-1}(X_n) = c_n - d_n X_n$ moves upward, increasing $SW_{n,2}$. In our model, this increase in demand decreases $Q_{n,min}$. Thus, the welfare could be improved. The impact on consumers surplus is less obvious as load-shedding increases prices in other periods. Its improvement relies on the level of elasticity of demand, impacting the hierarchical organization between price and volume effects.

Developing the above function, we obtain that $\Delta_n \geq 0$, i.e. DR is socially efficient, when the equilibrium quantity is in the optimal area defined below:

$$Q_n^* \geq Q_{n,\min} = \frac{2.SW_{n,1}}{c_n - a_n} \quad (15)$$

Q_n^* is the equilibrium effectively reached according to the supply and demand functions and the DR parameter, γ_n . $Q_{n,\min}$ is the minimum equilibrium quantity which could be reached with a DR scheme without a decrease in social welfare. This threshold exists for each equilibrium Q_n^* , i.e. for all configurations of the supply and demand functions. According to the supply and demand parameters, some of these equilibriums will induce a positive variation in social welfare.

As we also know that at intersection point *B* in Fig. 1, $Q_n^* = \frac{c_n - a_n}{\gamma_n + b_n + d_n}$, we can obtain a negative correlation between the intensity of the DR scheme, γ_n , and the probability of coping with $\Delta_n \geq 0$ as $\lim_{\gamma_n \rightarrow +\infty} Q_n^* = 0$. This result makes sense, since the greater the intensity of DR, the more consumption is reduced. It being optimal for the DR scheme to reach $Q_n^* \in [Q_{n,\min}, Q_{n,\max} = \frac{c_n}{d_n}]$ to maintain social-welfare gains, intensive DR should have a greater impact reducing both consumer surplus and the profits of firms which base their competitive strategy on their marginal costs. There is consequently no incentive to design a γ_n such as $Q_n^* < Q_{n,\min}$ because of social-welfare losses when the demand function is elastic. As Δ_n is an increasing function of Q_n , we could conclude that $Q_n^* = Q_{n,\min}$ is the minimal condition the equilibrium must meet to keep the gains from DR schemes.

According to this initial result, we can see that the minimum quantity is linked to the parameters of the supply function a_n and b_n , reflecting the marginal costs of supply, and reserve electricity prices before and after changes in consumer behaviour due to the DR scheme, $Voll_n$ and c_n , respectively.

2.2.2.1. Efficient country results.

Proposition 3. *If the country is efficient, there is an optimal area for which a demand response scheme does not reduce social welfare. This area is negatively correlated with the degree of competitiveness of the generation technologies and the size of the country's market.*

The intuition of Proposition 3 is the following. A large size of the market increases $Q_{n,\min}$. Indeed, if $K_{t,n}$ increases, cheap generation is then available to serve the demand. Thus, $SW_{n,1}$ will increase too. In the same way, high levels of \bar{D}_n increase $SW_{n,1}$. As a result, $Q_{n,\min}$ increases, which implies difficulties to achieve the condition $SW_{n,2} > SW_{n,1}$. Moreover, in this case, a great DR deteriorates profits of efficient generators because of the non-served energy. The price effect does not compensate losses in sales in the retail market (as DR reduces final demand). Consumers' surplus is also damaged because of rationing whereas cheaper generation is available to serve their demand.²⁰ Cheaper generation goes with higher $SW_{n,1}$. Here again, the condition $SW_{n,2} > SW_{n,1}$ is difficult to achieve. Thus, opportunities to improve welfare with cheap generation capacities are reduced.

From the other side, DR reduces the demand in efficient country *n*. Thus, efficient generators are willing to increase their exports towards inefficient country *m*. However, if the costs of interconnectors are high (or if transmission capacity is limited), they could not easily increase their export levels. Thus, $Q_{n,\min}$ will increase. Moreover, the efficiency of the overall interconnected market is reduced, a large

part of the residual demand being served by inefficient or less efficient generation.

To sum up, DR programs could reduce the welfare when generation technologies are efficient. A high level of inelastic demand or large efficient generation capacities increase these losses (because of high initial values of $SW_{n,1}$). High levels of DR could be implemented only if costs parameters b_n are high or for low values of \bar{D}_n (that have a decreasing impact on $SW_{n,1}$).

To demonstrate these results, we assume first that country *n* is more efficient than country *m*. This means that with or without price signals, only its generation technologies will be called to meet local demand.

Integrating our results from Proposition 2 into Eq. (15), the optimal minimum quantity is thus equal to:

$$Q_{n,\min} = \frac{\sum_t K_{t,n} - \alpha \cdot Q_m + \frac{P_{n,m}}{(\alpha-1) \cdot b}}{2-\alpha} = \frac{2.SW_{n,1}}{c_n - a_n} \quad (16)$$

The left term (from cost-minimization programs (5–8)) and the right term (from Eq. (15)) are equal at equilibrium. Any change in a parameter of one term will be accompanied by a proportional change in another parameter in the other term, guaranteeing that the above equality always holds and equilibrium is still the one in which efficient technologies are predominant. The link between the two terms is obtained through parameter b_n as detailed below.²¹

We can deduce from Eq. (16) that the borders of the optimal area depend on many parameters related to the configuration of the interconnected systems and technology specifications. We define three criteria to study the sensitivity of $Q_{n,\min}$ to the main parameters. The first one concerns the market size of the efficient country; it is impacted by $K_{t,n}$ and \bar{D}_n . Indeed, the greater these parameters become, the larger we may assume the system to be. The second indicator is the level of cost-efficiency of technologies. Supply-function parameters, such as a_n and b_n , fall into this category. The third indicator reflects the impact of the limitation on transmission capacity.

2.2.2.1.1. Market size. From Eq. (16), we observe that an increase in the size of the efficient country's market, either due to an increase in $\sum_t K_{t,n}$ or in \bar{D}_n , causes $Q_{n,\min}$ to increase; consequently reducing the optimal area of DR. Two reasons could explain this correlation. First, because country *n* is cheap, any increase in its technology capacity will lead, on the one hand, to an increase in the level of exports to country *m* and, on the other, will offer cheaper technologies to country *n*, reducing the slope of its energy mix (parameter b_n) and boosting initial social welfare $SW_{n,1}$. We thus obtain an identical increase on the left and right sides of Eq. (16). The optimal area of a DR scheme, which does not degrade social welfare, is therefore reduced.²² Secondly, the higher initial demand is, \bar{D}_n ,²³ the greater the reduction in generation required to cope with the DR target (for lower consumption). The impact on the profitability of producers is consequently negative, due to the higher value of their unused capacity. As for consumers, a higher \bar{D}_n means that captive demand is high enough to allow rationing of a large number of users by a DR scheme, without impacting negatively on their welfare.

As a preliminary conclusion, we may assume that intensive DR is constrained by the market size of the system because of the considerable impact on producers of the value of non-served energy. Consumer rigidity would not only undermine the efficiency of DR, it would also impact the producers, with a drop in profit. In this case, consumer rationing is costly for society. There is no need for consumers to be

²¹ This analysis procedure is followed for all the scenarios below.

²² $d \left(\frac{\sum_t K_{t,n} - \alpha \cdot Q_m}{2-\alpha} \right) > 0$ if $\alpha \cdot \frac{dQ_{n,m}}{dc_n} < 1$, meaning that only part of the capacity increase will be exported. At the same time, $\frac{dSW_{n,1}}{db_n} > 0$ because of decrease in b_n .

²³ $\frac{dSW_{n,1}}{d\bar{D}_n} > 0$ because $P_{n,1}^* = a_n + b_n \bar{D}_n < \bar{P}_n$.

²⁰ Chao (2011) has shown similar results by considering the incentive policies of DR to consumers. He concludes that if remuneration of DR is too high (called the "double remuneration"), it could be detrimental for welfare because DR is over-evaluated, by replacing cheaper generation, which is more efficient.

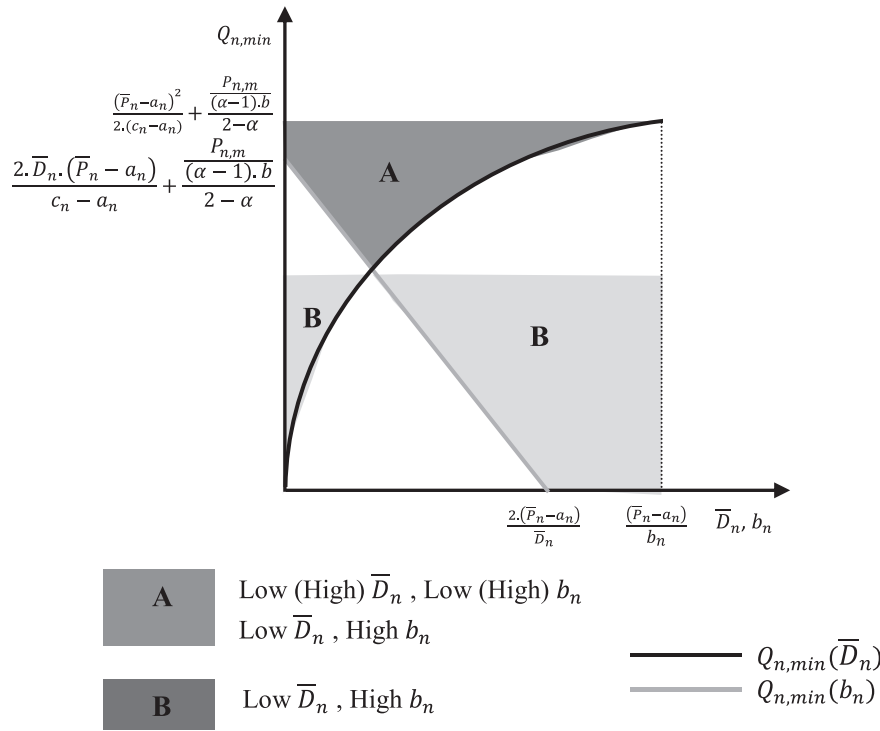


Fig. 2. Optimal regions of DR for efficient country.

rationed or adapt their consumption, generation being available and cheap. Indeed, the loss in terms of surplus could be very high in a situation where generation is cheap but consumption must decrease because of the voluntary price increase. There is a kind of opportunity cost for rationing consumers without constraining the system.

2.2.2.1.2. *System-cost efficiency.* The second group of parameters regarding cost efficiency comprises parameters specific to the supply function (a_n and b_n). Again, when a_n or b_n decreases, which also means that technologies are increasingly efficient, we observe an increase in $Q_{n,min}$. Indeed the cost of serving demand \bar{D}_n with an efficient energy mix is now lower. Intensive DR would entail a higher opportunity cost which in turn would limit DR efficiency.

2.2.2.1.3. *Transmission-capacity limit.* Due to the constraint on interconnection capacity, a capacity price effect associated with use of the interconnection is represented by $\frac{P_{n,m}}{(\alpha-1)b}$. The higher the value of interconnection capacity, the smaller the optimal DR area becomes. Intensive DR should encourage consumers to greatly reduce their consumption. Such a reduction in consumption will be accompanied by a large drop in local generation. However, efficient producers, seeing a huge reduction in the volume they generate, can export surplus production to the less efficient neighbouring country, thus reducing the negative volume effect of such a measure. But when interconnection capacity is limited and access to it is more expensive, export becomes both more costly and less feasible. Hence, the equilibrium at which the greatest possible use is made of efficient technologies is much more difficult to reach. The cost of serving rationed demand will significantly increase, prompting the system operator to adopt a less intensive DR scheme to prevent system collapse.

2.2.2.1.4. *Optimal system configuration for intensive demand response.* To conclude we shall look at two indicators reflecting the cost structure and the market size of the studied country. The first one includes, as stated previously, parameters such as the supply-function parameters, a_n and b_n . As we have shown, the impact of these parameters on $Q_{n,min}$ is the same: the more cost-efficient technologies are, the higher $Q_{n,min}$ becomes. So, for simplicity's sake, we can focus exclusively on parameter b_n , as a good indicator of the cost efficiency of the technologies.

Regarding the market size indicator, we should emphasize that the higher initial captive demand \bar{D}_n , or generation capacity $\sum_t K_{t,n}$, is, the higher $Q_{n,min}$ becomes. For greater simplicity, we shall centre our conclusion on the impact of \bar{D}_n . Fig. 2 shows the variation in the optimal area depending on the levels of b_n and \bar{D}_n .²⁴ The curves are approximated, based on our results from Eqs. (15) and (16).

Two zones can be identified. The first zone A means that with low b_n and low \bar{D}_n , it is not possible substantially to reduce demand. If b_n is sufficiently low, rationing will lead to a high negative price effect on consumers. With low demand, the scheme would not yield a significantly positive quantity effect. In the opposite case, if both parameters are high, the volume effect is considerable compared to the price effect. In other words, the drop in generation yields an initial effect, with a second effect caused by the higher value of unused capacity. Finally, a slight reduction in demand is also expected when b_n is low and \bar{D}_n high. Whereas the positive volume effect for consumers would be offset by the high negative price effect, producers would lose a large amount of their surplus, as in the previous case because of the significant drop in generation reduction and higher value of unused capacity. However, the positive impact of the price increase on producers would be limited, given the increasing impact of the DR scheme on operating costs.

However, an aggressive DR scheme could only be deployed if b_n was high and \bar{D}_n low (zone B in Fig. 2). To more reduce consumption without welfare losses, the negative volume effect of the DR scheme on consumers and producers must be offset by the positive price effect, yielding an insignificant impact on total surplus.

2.2.2.2. *Inefficient country.*

Proposition 4. *If a country is inefficient, the more it imports, the less effective intensive DR will be.*

The intuitions of Proposition 4 are as follows. Costs and \bar{D}_n have the same impact as in the previous case (efficient country). However,

²⁴ We disregard extreme situations, i.e. when the country becomes inefficient compared to its neighbour. Such a situation will be studied in the next subsection.

imports are now playing a major role. We could see that the DR intensity is a decreasing function of imports from the efficient country. Indeed, if these imports are large, thus $SW_{n,1}$ is great which makes it difficult to satisfy $SW_{n,2} > SW_{n,1}$. We could conclude that if interconnection prices are high (or for low interconnection capacities), the DR could also be high ($SW_{n,1}$ is reduced and the condition $SW_{n,2} > SW_{n,1}$ is easily satisfied). A more aggressive DR could also be implemented if b_n is high (reflecting high generation cost in country n) or for low values of $K_{t,m}$ (imports from efficient country are reduced). Indeed, in that case, consumers are served by costly generation. If they cannot import cheaper energy, thus $SW_{n,1}$ is reduced and $Q_{n,min}$ decreases, facilitating the satisfaction of $SW_{n,2} > SW_{n,1}$.

To demonstrate these results, we shall now assume that country n is less efficient than country m . This means that with or without price signals, it always relies on imports from country m to satisfy local demand.

The minimum quantity for efficient DR is equal to:

$$Q_{n,min} = \frac{\sum_t K_{t,m} - \alpha Q_m - \frac{\alpha^2}{\alpha-1} \cdot b \cdot \sum_m P_{m,n} + Res_n}{2-\alpha} = \frac{2 \cdot SW_{n,1}}{c_n - a_n} \quad (17)$$

Parameters a_n and b_n (through $SW_{n,1}$) have the same effect on $Q_{n,min}$. Any decrease in the inefficiency of the cost of the technologies positively impacts $Q_{n,min}$. Similarly, the market-size indicator of the inefficient country, \bar{D}_n , through $SW_{n,1}$, stills positively influences $Q_{n,min}$. The optimal area is however significantly influenced by the market size of the exporting country m , i.e. $K_{t,m}$, as we will see next. As a preliminary interpretation, we can say that since the country relies massively on imports, any local energy policy would be subject mainly to the attractiveness of imports.

2.2.2.2.1. Market size of the exporting country. When the level of generation capacity in the exporting country, $K_{t,m}$, rises, so does $Q_{n,min}$. DR in the inefficient importing country becomes less effective. An increase in $K_{t,m}$ will relax the neighbouring system, therefore encouraging higher exports to the inefficient system. Two situations are consequently possible. The inefficient technologies in country n may be more replaced by less costly ones, so that an increase in $K_{t,m}$ will be accompanied by a decrease in the residual demand served by local producers, Res_n , with quite limited impact on $Q_{n,min}$. Alternatively, the growth in capacity in the exporting country will be transferred to country n , thus satisfying more demand. $Q_{n,min}$ must increase because Res_n will still be unchanged. In the latter case, rationing is more harmful for consumers. Indeed, when available capacity is competitive, consumers do not need to be rationed or adapt their consumption, generation being cheap. The opportunity cost of rationing consumers without constraining the system is significant here.

2.2.2.2.2. Transmission-capacity limit. Eq. (17) shows that the greater the cost of imports for the inefficient country, the more intensive DR could be. Indeed, when $P_{m,n}$ increases, there is less scope for relying on imports to satisfy local demand. Inefficient local generation will be used to balance the system. Given that the opportunity cost of reducing generation is much lower for inefficient technologies (local producers) than efficient ones (exporters), the system operator can deploy a more aggressive DR scheme without facing the social cost of unserved generation entailed by relying only on efficient technologies.

2.2.2.2.3. Optimal system configuration for intensive demand response. To conclude, we shall again focus on two criteria relating to the cost level of technologies in the inefficient country and to the market size of the exporting country, given that it significantly influences equilibrium in the studied market. We consider the parameter b_n as an indicator of the country's efficiency. We look at the impact of $K_{t,m}$ as an indicator of the market size of the neighbouring country counterbalancing the inefficiency of the studied country. Fig. 3 shows the optimal area of DR with regard to b_n and $K_{t,m}$.

Here, three zones are identified. Zone A means that it is socially inefficient to target low demand-reduction when either b_n or $K_{t,m}$ are low or only $K_{t,m}$ is high. If b_n and $K_{t,m}$ are low, this means that the system is less inefficient but cannot rely as much on imports. On the one hand, there is less scope for rationing consumers, generation being cheap. On the other, the system operator must rely on local producers to satisfy local demand, so intensive demand-reduction would have a negative impact on welfare due to the DR scheme's high negative price effect on producer surplus, i.e. the large price differential between the initial situation and the target scenario. If $K_{t,m}$ is high, imports could be abundant regardless of the system's cost-intensity. DR is also limited. Whereas consumers could be less sensitive to demand rationing, the significant weight of cheap imports will induce a significant decrease in their surplus, making the large-scale demand reduction socially inefficient for all actors involved in a system of this sort. This result is very interesting and emphasizes the extent to which the development of interconnections between countries could condition energy strategies in countries heavily dependent on energy imports.

However, an aggressive DR scheme could only be deployed if b_n is high and $K_{t,m}$ is low (zone B). In this case, a very inefficient system coexists with a low rate of imports. In such a case, consumers would be more inclined to accept demand rationing, the electricity price already being excessive. On the other hand, local producers and importers would not see a significant drop in their surplus, making aggressive demand reduction socially acceptable regarding the interests of the actors involved in such a system. This means that intensive DR could be deployed if the system was already extremely inefficient and also relatively isolated.

These results are summarized in Table 1.

3. Consumer-surplus analysis

We shall now study the extent to which the optimal area for DR schemes would vary if, instead of social welfare, we consider variations in consumer surplus. Consumers are sensitive to financial losses that could occur with the adoption of a new technology (Park et al., 2014). In the case of a smart grid being deployed with demand response schemes and dynamic pricing, these fears would be associated with lower surplus, because of the risk of higher electricity bills.²⁵ This is one of the main risks that consumer groups fear when DR schemes are introduced. Indeed, a DR mechanism must act mainly on consumer profiles; its efficiency depends on their willingness to adapt and the elasticity the DR scheme can activate. The impact on consumer surplus is a major social constraint, which the authorities should take into account when trying to modify the rational equilibrium of their energy systems.

Proposition 5. *If variation in consumer surplus, rather than social welfare, was used as the key criterion, more aggressive DR could be adopted, unless the system was cost-inefficient and captive demand is low.*

Intuitively, if consumer's demand is high, they could reduce it easier. Moreover, for costly generation technologies, their energy bills are high. Thus, consumers would modify their consumption (they decrease it) to reduce their payments. Choosing greater values of γ_n would be optimal, as we made the assumption of the positive correlation between the level of investment costs in smart appliances and demand reduction. With a consumer's surplus analysis, losses of the generators' side are not considered, leading then to sustain the benefits of greater demand response.

²⁵ SG and DR pilots have shown that this risk exists but could be limited for consumers who react to signals from utilities or DSOs (Faruqui et al., 2007, 2011; Faruqui and Sergici, 2010).

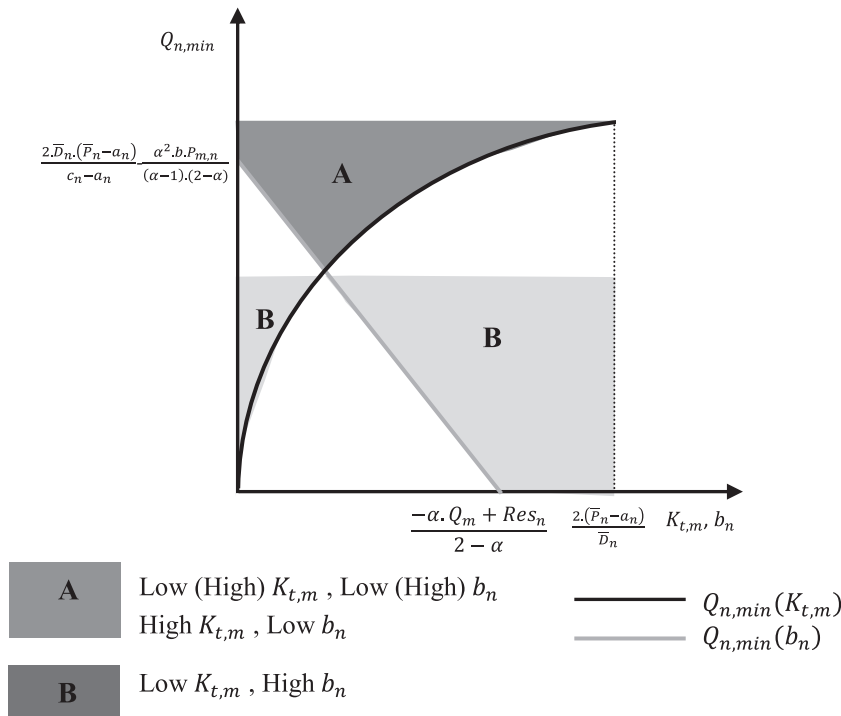


Fig. 3. Optimal regions of DR for inefficient country.

To show these results, we define Ω_n as the variation in consumer surplus after deploying a DR scheme:

$$\Omega_n = CS_{n,2} - CS_{n,1} \tag{18}$$

$CS_{n,1} = \int_{P_n}^{P_n^{voln}} (\bar{D}_n) dP_n$ consumer surplus at equilibrium before deploying a DR scheme.

$CS_{n,2} = \int_{P_n}^{c_n} (D_n(P_n)) dP_n$ consumer surplus at equilibrium after deploying a DR scheme.

Developing the above function,²⁶ we obtain that $\Omega_n \geq 0$, i.e. DR is efficient from the consumers' point of view, when the equilibrium quantity falls within the optimal area below:

$$Q_n^* \geq Q_{n,min} = \sqrt{\frac{2 \cdot CS_{n,1}}{d_n}} \tag{19}$$

It would be possible to reduce consumption without decreasing consumer surplus as far as $Q_{n,min}$ in Eq. (19) above. We can verify that DR intensity is positively correlated to the elasticity of the demand function and negatively correlated to captive-demand prices. If we assume that the authorities mainly consider the impact in terms of consumer surplus, we can demonstrate that a higher reduction in consumption could be obtained if the following condition was met²⁷:

$$\sqrt{\frac{2 \cdot CS_{n,1}}{d_n}} \leq \frac{2 \cdot SW_{n,1}}{c_n - a_n} \tag{20}$$

In what follows, we shall look at the additional reduction in consumption which could be achieved subject to a consumer-surplus constraint by focusing on two parameters: the system's cost efficiency

²⁶ $\Omega_n \geq 0$ if $Q_n \cdot (\frac{c_n - P_n}{2}) \geq CS_{n,2}$. Given that $P_n = c_n - d_n \cdot Q_n$, then $Q_{n,min} = \sqrt{\frac{2 \cdot CS_{n,1}}{d_n}}$.

²⁷ If $Q_{n,min}$ subject to consumer-surplus criteria is higher than $Q_{n,min}$ subject to social-welfare criteria.

Table 1
Impact of DR programs on welfare with efficient or inefficient country.

	Welfare improvement with DR	No welfare improvement with DR
Efficient country (n)	Low values of $K_{t,m}$ or \bar{D}_n High values of costs or $P_{n,m}$	High values of $P_{n,m}$, $K_{t,m}$ or \bar{D}_n Low values of costs
Inefficient country (n)	High values of $P_{n,m}$ High values of costs and low values of $K_{t,m}$	High values of $K_{t,m}$ or low values of $K_{t,m}$ Low values of costs and $K_{t,m}$

and market size, respectively, b_n and \bar{D}_n .²⁸ The results shown in Fig. 4 confirm our previous results regarding the impact of consumer surplus on variation in social welfare, via the price and the volume effects of the DR scheme. The figure yields two main conclusions. First, when the market size of the system is high, i.e. high \bar{D}_n , as shown in the right-hand part of Fig. 4, and regardless of the level of cost efficiency, a higher reduction in consumption could be reached if only the impact on consumer surplus is considered (zone B in the right-hand part of Fig. 4). This additional reduction in quantity could also be obtained if demand was moderate, but the system must be highly inefficient in terms of cost (zone B in the left-hand part of the figure). Indeed, if demand is very high, the negative price effect of intensive DR on consumers would be offset by the positive volume effect. On the other hand, for producers, the positive price effect being insignificant (price variation is low due to the additional cost of DR), the negative price effect would substantially reduce their own surplus. DR could consequently not be intensive. Likewise, if demand was not high enough, DR could only be intensive if the system was expensive. In which case, consumers already paying high bills would be more inclined to accept aggressive demand reduction, the volume effect being higher than the price effect.

²⁸ Detailed analysis of the impact of the interconnection-capacity price is disregarded here. As before, if interconnection capacity is constrained, the optimal area is reduced when the system is efficient and otherwise increased. This holds when subject to both social-welfare and consumer-surplus criteria.

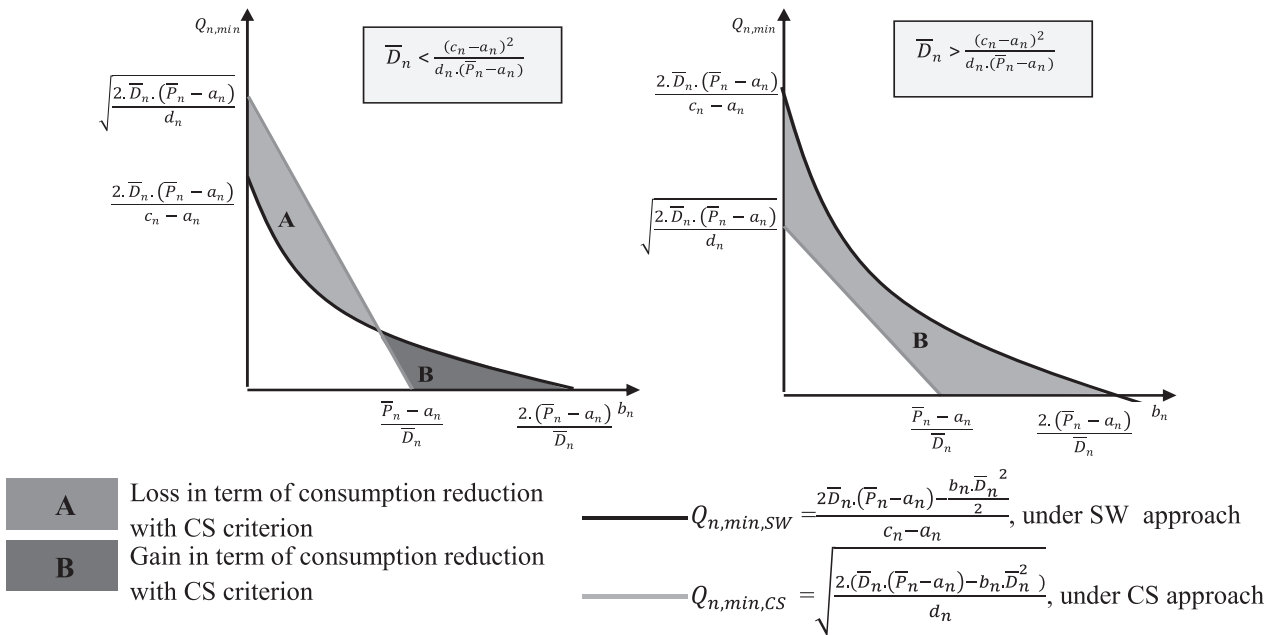


Fig. 4. Maximal consumption reduction under consumers' surplus criterion and social welfare criterion.

The second conclusion is that, with an approach focusing on consumer surplus, we cannot expect a major reduction in consumption if the system is already cheap and demand is low (zone A in the figure). Again, the negative price effect of the measure would be high enough for consumers and demand rationing would be less acceptable, energy being cheap and their consumption already low.

The results on the impact of DR on consumer surplus are summarized in Table 2.

4. Demand response and elasticity of demand

We end our analysis by studying the sensitivity of our results to elasticity of demand. We look at the reduction in consumption a DR scheme could achieve at a given level of elasticity. Various situations are considered regarding the cost efficiency and market size of the country as well as its degree of interconnection with the neighbouring country.

Proposition 6. *Elasticity of demand is negatively correlated to the intensity of the DR scheme. In general, less elastic demand is needed under a consumer-surplus approach. Finally, the more efficient the system is, the more elastic consumer-demand must be, to sustain DR efficiency.*

With efficient DR, i.e. that improves consumer surplus and welfare, demand should be elastic, particularly if generation technologies are efficient because of an increase in $SW_{n,1}$. The elasticity of demand increases $SW_{n,2}$ and could compensate high values of $SW_{n,1}$. In this case, $Q_{n,min}$ decreases with the elasticity of demand.

To demonstrate these results, we define \mathcal{E}_n as the level of demand elasticity in country n after DR has been deployed:

$$\mathcal{E}_n = Q'(P_n) \cdot \frac{P_n}{Q_n} \tag{21}$$

A DR scheme is efficient when elasticity falls within the following area²⁹:

$$\mathcal{E}_n \geq 1 - \frac{c_n}{d_n \cdot Q_{n,min}} \tag{22}$$

²⁹ From Eq. (21) and knowing that $P_n = c_n - d_n \cdot Q_n$, we find $\mathcal{E}_n = 1 - \frac{c_n}{d_n \cdot Q_n}$. Efficient DR is when $Q_n \geq Q_{n,min}$, so $\mathcal{E}_n \geq 1 - \frac{c_n}{d_n \cdot Q_{n,min}}$.

where,

$$Q_{n,min} = \begin{cases} \frac{2 \cdot SW_{n,1}}{c_n - a_n} & \text{If social welfare criterion is used} \\ \sqrt{\frac{2 \cdot CS_{n,1}}{d_n}} & \text{If consumers' surplus criterion is used} \end{cases}$$

Fig. 5 prompts three main comments. Firstly, the greater the elasticity of demand, the more aggressive DR could be, i.e. $Q_{n,min}$ decreases, whatever the efficiency of the system and under both criteria. Indeed, when demand is increasingly elastic, consumers are more inclined to reduce consumption after a given price increase. Secondly, demand elasticity has less impact on reducing consumption if social welfare is considered rather than consumer welfare, i.e. the shift in demand reduction to the left from the black curve to the gray one in the figures, unless the system is cost-efficient with greater market size. For a given reduction in quantity, higher elasticity of demand would be needed under an approach enhancing welfare than for one raising consumer surplus. This additional elasticity is needed to compensate for the loss of producer surplus induced by the DR scheme. Finally, when the system is efficient and export is less possible, the cost of serving the rationed demand is greater. The un-exported quantity—excess generation—must be injected into the system, with a dual impact. The first is to increase the merit-order function; the second is to increase local generation in order to balance the system with its cheap, efficient technologies. A larger quantity must now be produced at a probably higher cost because un-exported generation may be more expensive. Even consumer surplus will be negatively impacted, energy being more expensive.

The opposite phenomenon is observed when the system is inefficient and relies massively on imports. Under the consumer-surplus

Table 2
Impacts of DR on consumer surplus.

	Consumer surplus improvement with DR	No consumer surplus improvement with DR
Efficient or inefficient country	High values of \bar{D}_n or of costs Intermediate values of \bar{D}_n and high values of b_n	Low values of \bar{D}_n Low values of costs

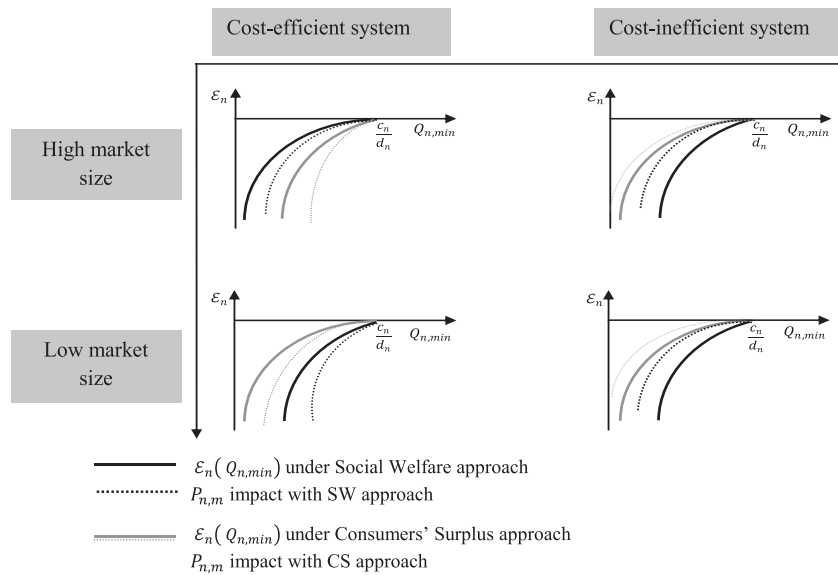


Fig. 5. Elasticity of demand and optimal consumption reduction.

Table 3
Impact of elasticity of demand variation on DR program efficiency with welfare and consumer surplus scenarios.

Welfare	Consumer surplus
Lower DR intensity can be reached with the welfare case compared to the consumer surplus case regardless the level of elasticity of demand	
Greater DR programs for high values of elasticity is possible in all scenarios for any costs level	
Elasticity have less impact on DR values (unless efficient technologies and high market size)	Elasticity have more impact on DR values (unless efficient technologies and high market size)
Great elasticity of demand is needed to compensate suppliers losses	Low elasticity of demand is needed for DR to be efficient

approach, before the DR scheme is deployed, consumer surplus is low due to the lack of efficient generation. With the DR scheme, energy becomes more expensive than in a situation where imports are free. To cover the increased loss in their surplus due to the rising negative price effect, consumers would accept a higher cut in consumption and benefit from a more positive volume effect, which explains why we also see a higher reduction in quantity under the consumer-surplus approach.

Results of the elasticity of demand analysis are summarized in Table 3.³⁰

5. Conclusion

This paper aims to demonstrate analytically the conditions under which activating the elasticity of consumer demand could benefit social welfare. It supplements the literature analysing the use of price signals to elicit demand response. Initial analysis focused on how the structure of generation technologies could affect the merit orders of countries and potential trade between them. The results show that the trade-off between producing locally and exporting energy depends on the opportunity cost of the energy and the overall efficiency of the generation technology. We have demonstrated that interconnection prices would have negative impacts on trades, regardless of their destination. This result also relies on the generation-cost differential between the

interconnected systems. Indeed, if countries have significant cost differentials in generation technologies, a decrease (or increase) in imports (exports) linked with interconnection prices and exchange capacities impacts welfare and DR intensity.

Our second analysis demonstrated that there is an optimal area for the price signal, at which demand response increases social welfare. This optimality area is negatively correlated with the degree of competitiveness of the generation technologies and the market size of the system. While the literature and policy recommendations have widely highlighted that the degree of consumers' ability to adapt their behaviour is the prime condition affecting the effectiveness of a demand response scheme, the present work has demonstrated that the impact on producer surplus must be considered as a constraint on deploying demand response. More specifically, the value of unserved energy or energy reduction the producers could lose from such a reduction in consumption would limit the implementation of a scheme of this sort. Furthermore, this constraint is greater if energy trade between countries is limited. However, this constraint is alleviated if the considered system in cost-inefficient as well as weakly connected with its neighbours. Our intuition was confirmed when analysis only considered the impact in terms of consumer surplus instead of social welfare. We demonstrated that under such conditions, more aggressive DR could be adopted, the weight of producer welfare being removed. Finally, our analysis has demonstrated that the intensity of a demand response scheme is negatively correlated to the degree of demand elasticity. But more elastic demand is needed if consumer surplus is the considered criteria.³¹

This paper could be extended in several ways. Firstly, strategic interaction between producers, which should affect merit-order functions and consequently market equilibrium, needs to be introduced. Secondly, consumer behaviour could be more robustly analysed by integrating their satisfaction as energy consumers with a form of utility function. Consumers should also be distinguished by type and consumption profile.

Appendix A. Supplementary data

Supplementary data to this article can be found online at <http://dx.doi.org/10.1016/j.eneco.2015.10.013>.

³⁰ As we said before, the γ_n parameter leads consumers to benefit from smart technologies to easily respond to price signal. Thus, their elasticity could increase with this opportunity while the condition in Eq. (22) could more likely to be satisfied.

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